

uPVC PENSTOCK LOSSES & THICKNESS CALCULATION

SITE NAME

Sample

Quantity

Symbol

Unit

PENSTOCK LOSS CALCULATIONS

Input Data

Flow	Q	70 l/s
Gross head	H_g	22 m
Penstock length	L	60 m
Penstock internal diameter	d	190 mm

Calculations

Velocity in penstock $V = 1.273 \cdot \left(\frac{Q}{d^2}\right) = 2.47 \text{ m/s}$

Friction head loss in penstock $H_f = 12.8 \times \left(\frac{V^2 \cdot L}{d}\right) \times \frac{1}{\left(\log\left[\frac{1}{370d} + \frac{1}{(93.8 \cdot V \cdot d)^{0.9}}\right]\right)^2} = 1.46 \text{ m}$

Net head at end of penstock $H_n = H_g - H_f = 20.5 \text{ m}$

Penstock efficiency $\eta_{pen} = \frac{H_n}{H_g} \times 100 = 93.3 \%$

PENSTOCK THICKNESS CALCULATIONS

Input Data

Penstock thickness	t	4.7 mm
% of flow stopped	z	50 %
valve closure time	T_{close}	0.1 s
Overall safety factor	SF_{tot}	3

Calculations

Wave velocity in penstock $V_{wave} = \sqrt{\frac{2 \cdot 8 \times 10^6 \cdot t}{(1.33t + d)}} = 259 \text{ m/s}$

Penstock critical time $T_{crit} = \frac{2L}{V_{wave}} = 0.46 \text{ s}$

Surge head for $T_{close} \leq T_{crit}$ $H_{surge} = \frac{V_{wave} \cdot z \cdot V}{980} = 32.6 \text{ m}$

OR

For $T_{close} \geq T_{crit}$ $K_c = \left(\frac{L \cdot z \cdot V}{980 H_g \cdot T_{close}}\right)^2 = 11.8$

Surge head for $T_{close} \geq T_{crit}$ $H_{surge} = H_g \cdot \left(\frac{K_c}{2} + \sqrt{K_c + \frac{K_c^2}{4}}\right) = - \text{ m}$

Total head at surge $H_{tot} = H_{surge} + H_g = 54.6 \text{ m}$

Required penstock thickness $t_{req} = \frac{H_{tot} \cdot d \cdot SF_{tot}}{5,710} = 5.45 \text{ mm}$

Values of Constants Used

Gravity	g	9.8 m/s
Bulk modulus of water	K_w	2.1 kN/mm ²
Density of water	ρ_w	1000 kg/m ³
Kinematic viscosity of water (5°C)	ν_w	1.53 cSt
Penstock roughness coefficient	k	0.01 mm
Penstock Young's Modulus	E_p	2.8 kN/mm ²
Penstock UTS	σ_{ult}	28 N/mm ²